Abstract

We investigate the outcome of performing world record sports events on the Moon with reduced gravity. We studied men’s shotput and 100 m sprint; held by Randy Barnes (23.12 m) and Usain Bolt (9.58 s) respectively. After calculating the world records attempts on the moon, we found that the shotput record would increase to 168 m and the 100 m sprint record would slow to 10.0 s.

Introduction

In this paper, we investigate how world record attempts for shotput and sprinting would differ if attempted on the Moon. We expect that the shotput record will improve and the sprint will worsen. We have analysed the dynamics of the sports to test the outcome of reduced gravity. We assume that the athletes engage in their respective sports immediately after landing on the Moon to prevent any muscle mass loss and that the athletes have the same oxygen capacity as on Earth, wearing protective suits of negligible mass.

Theory

In shotput, Randy Barnes holds the current world record with a distance of 23.12m [1]. To calculate the theoretical Moon record attempt, we assume the shot is thrown from the height of Randy Barnes 1.95m at an angle of 40 degrees, the optimum angle when throwing a shot [2], which has been assumed to be independent of gravity.

We combine equations 1 and 2, and rearrange to find the initial velocity of the shot during the world record attempt, as shown in equation 3.

\[ x = ut \cos(\theta) \] (1)
\[ y = y_0 + ut \sin(\theta) + \frac{1}{2} at^2 \] (2)
\[ u = \sqrt{-\frac{1}{2} ax^2 \frac{1}{y_0 + x \tan(\theta) \cos(\theta)}} \] (3)

On the Moon, assuming the same initial velocity of the shot, we use equation 4 to calculate the height that the shot would reach.

\[ y_{max} = \frac{v^2 - (u \sin(\theta))^2}{2a} \] (4)

where \( y_{max} \) is the height the shot will reach and \( v \) is the final velocity of the shot.

We calculate the total time of flight of the shot using equations 5 and 6 for the shot travelling up then down respectively.
\[ t = \frac{v - u}{a} \]  
\[ t = \frac{-u \pm \sqrt{u^2 - 4\left(\frac{1}{2}a\right)(s)}}{2\left(\frac{1}{2}a\right)} \]

This time of flight and the horizontal component of the initial speed of the shot in equation 7 are used to calculate the horizontal distance the shot would travel.

\[ x = uT \]

where \( T \) is the total time of flight calculated by taking the sum of equations 5 & 6.

Usain Bolt is the current world record holder for the 100m sprint with a time of 9.58s [3]. When Usain Bolt runs, he takes, on average, 41 strides over 100m [3]. We assume Usain’s leg is lifted 0.7m with each stride.

We start by calculating the deceleration of half a stride, that is, Usain’s leg from the top of his stride to the floor. We split the acceleration into two components coming from the force due to gravity and the force provided by his leg muscles.

Using equation 8 we found the acceleration due to Usain’s leg muscles.

\[ x = vt - \frac{1}{2}at^2 \]  

We use equation 8 again, this time rearranging for time. This is multiplied by 82 to obtain the time taken for the 100m sprint.

Discussion

We find the initial velocity of the shot to be 14.6m\(s^{-1}\) on the Earth. On the Moon, we find the maximum height of the projectile is 27.1m. We find the time of flight for the shot to be 15.0s. From this, the shotput Moon record would be 168m. The range calculated for the shot is larger than expected but when considering the difference in gravity, does seem reasonable. The record for shotput would be much improved on the Moon according to our calculations but in reality Barnes’ technique could be affected in an unfamiliar environment if the world record was attempted.

For the 100m sprint, we find the time per half a stride on the moon to be 0.122s which gives a total time of 10.00s. This is only slightly slower than on Earth. This is justified since in sprinting the main power comes from Bolt driving his feet into the ground and he would not be vastly affected by the decreased gravity. Sprinting is more difficult to model simply than shotput so aspects of friction and drag have been neglected in this paper and should be analysed to improve this result.

Conclusion

We have looked at the difference in sports on the Earth and Moon by comparing shotput and 100m on both planets. Our projectile calculations find that the world record for shotput would improve from 23.12m on Earth to 168m on the Moon. The acceleration due to gravity influences the height and range of a shotput ball massively for this result. The world record for 100m sprint would slow down from 9.58s to 10.0s. It is worth noting that this result may differ if friction were taken into account, so this is suggested as future work in this area, however is beyond the scope of this paper.

References


